# **BOARD QUESTION PAPER : MARCH 2022** MATHEMATICS AND STATISTICS

#### Time: 3 Hrs.

Max. Marks: 80

The question paper is divided into FOUR sections.

- (1) Section A: Q.1 contains Eight multiple choice type of questions, each carrying Two marks. Q.2 contains Four very short answer type questions, each carrying one mark.
- (2) Section B: Q.3 to Q. 14 contain Twelve short answer type questions, each carrying Two marks. (Attempt any Eight)
- (3) Section C: Q.15 to Q. 26 contain Twelve short answer type questions, each carrying Three marks. (Attempt any Eight)
- (4) Section D: Q.27 to Q. 34 contain Eight long answer type questions, each carrying Four marks. (Attempt any Five)
- (5) Use of log table is allowed. Use of calculator is not allowed.
- (6) Figures to the right indicate full marks.
- (7) Use of graph paper is <u>not</u> necessary. Only rough sketch of graph is expected.
- (8) For each multiple choice type of question, it is mandatory to write the correct answer along with its alphabet, e.g. (a)....../(b)....../(c)....../(d)....., etc. No marks shall be given, if <u>ONLY</u> the correct answer or the alphabet of correct answer is written. Only the first attempt will be considered for evaluation.
- (9) Start answer to each section on a new page.

### **SECTION – A**

at answer for the following multiple shoirs type of an

| Q.1. |       |   |  |                                  |  | [16]                |  |     |                 |     |
|------|-------|---|--|----------------------------------|--|---------------------|--|-----|-----------------|-----|
|      | (i)   |   | $\sim p \land (\sim q \rightarrow$                                 |                                  | → 1) 15 <u> </u>   | (h)                 | $p \lor (\sim q \lor r)$                                     |     |                 |     |
|      |       |   | $\sim p \land (\sim q \rightarrow q)$                              | · · · ·                          |  |                     | $p \rightarrow (q \wedge r)$<br>$p \rightarrow (q \wedge r)$ |     |                 | (2) |
|      | (ii)  | In Λ/   | ABC if $c^2 + a$   | $a^2 - b^2 =$                    | = ac, then $\angle B$ =  |                     | ,  |     |                 |     |
|      | ()    |   | $\frac{\pi}{4}$  |                                  |  | (c)                 | $\frac{\pi}{2}$  | (d) | $\frac{\pi}{6}$ | (2) |
|      | (iii) | Equation of line passing through the points $(0, 0, 0)$ and $(2, 1, -3)$ is |  |                                  |  |                     |  |     |                 |     |
|      |       | (a)   | $\frac{x}{2} = \frac{y}{1} = \frac{z}{-3}$                         |                                  |  | (b)                 | $\frac{x}{2} = \frac{y}{-1} = \frac{z}{-3}$                  |     |                 |     |
|      |       | (c)   | $\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$                          |                                  |  | (d)                 | $\frac{x}{3} = \frac{y}{1} = \frac{z}{2}$                    |     |                 | (2) |
|      | (iv)  | The v   | value of $\hat{i} \cdot (\hat{j})$                                 | $(\times \hat{k}) + \hat{j}$     | $\hat{j} \cdot (\hat{k} \times \hat{i}) + \hat{k} \cdot (\hat{i} \times \hat{j})$ is |                     |  |     |                 |     |
|      |       | (a)   | 0  | (b)                              | -1   | (c)                 | 1  | (d) | 3               | (2) |
|      | (v)   | If f(x  | $=x^{5}+2x-$   | 3, then                          | $(f^{-1})'(-3) =$  | ·                   |  |     |                 |     |
|      |       | (a)   | 0  | (b)                              | -3   | (c)                 | $-\frac{1}{3}$   | (d) | $\frac{1}{2}$   | (2) |
|      | (vi)  | The r   | naximum va   | lue of t                         | he function $f(x) = \frac{\log x}{x}$  | $\frac{3x}{2}$ is _ | ·  |     |                 |     |
|      |       | (a)   | e  | (b)                              | $\frac{1}{e}$  | (c)                 | e <sup>2</sup>   | (d) | $\frac{1}{e^2}$ | (2) |
|      | (vii) | If $\int_{\overline{4}}$  | $\frac{\mathrm{d}x}{\mathrm{d}x^2 - 1} = \mathbf{A}  \mathrm{loc}$ | $\log\left(\frac{2x}{2x}\right)$ | $\left(\frac{-1}{+1}\right)$ + c, then A =   |                     |  |     |                 |     |
|      |       | (a)   | 1  | (b)                              | $\frac{1}{2}$  | (c)                 | $\frac{1}{3}$  | (d) | $\frac{1}{4}$   | (2) |
|      |       |   |  |                                  |  |                     |  |     |                 |     |

[17]

#### Std. XII: Mathematics and Statistics

Q.2.

|   | (viii) | If the p.m.f of a r.v.X is  |                             |                       |     |
|---|--------|---|-----------------------------|-----------------------|-----|
|   |        | $P(x) = \frac{c}{x^3}$ , for $x = 1, 2, 3$                              |                             |                       |     |
|   |        | = 0, otherwise,   |                             |                       |     |
|   |        | then $E(X) =$   |                             |                       |     |
|   |        | (a) $\frac{216}{251}$ (b) $\frac{294}{251}$                             | (c) $\frac{297}{294}$       | (d) $\frac{294}{297}$ | (2) |
| • | Ansv   | ver the following questions:  |                             |                       | [4] |
|   | (i)    | Find the principal value of $\cot^{-1}\left(\frac{-1}{\sqrt{3}}\right)$ |                             |                       | (1) |
|   | (ii)   | Write the separate equations of lines re                                | presented by the equation 5 | $5x^2 - 9y^2 = 0$     | (1) |

- (iii) If  $f'(x) = x^{-1}$ , then find f(x)
- (1)(iv) Write the degree of the differential equation  $(y''')^{2} + 3(y'') + 3xy' + 5y = 0$ (1)

#### **SECTION – B**

#### Attempt any EIGHT of the following questions: **Q.3.** Using truth table verify that:

 $(p \land q) \lor \sim q \equiv p \lor \sim q$ 

[16]

(2)

(2)

[24]

(3)

- **Q.4.** Find the cofactors of the elements of the matrix  $\begin{vmatrix} -1 & 2 \\ -3 & 4 \end{vmatrix}$ (2)
- **Q.5.** Find the principal solutions of  $\cot \theta = 0$ (2)**Q.6.** Find the value of k, if 2x + y = 0 is one of the lines represented by  $3x^2 + kxy + 2y^2 = 0$ (2)**Q.7.** Find the cartesian equation of the plane passing through A(1, 2, 3) and the direction ratios of whose
- normal are 3, 2, 5. (2)
- **Q.8.** Find the cartesian co-ordinates of the point whose polar co-ordinates are  $\left(\frac{1}{2}, \frac{\pi}{3}\right)$ . (2)
- **Q.9.** Find the equation of tangent to the curve  $y = 2x^3 x^2 + 2$  at  $\left(\frac{1}{2}, 2\right)$ . (2)
- **Q.10.** Evaluate:  $\int_{0}^{4} \sec^{4} x \, dx$ (2)
- **Q.11.** Solve the differential equation  $y \frac{dy}{dx} + x = 0$ (2)
- **Q.12.** Show that function  $f(x) = \tan x$  is increasing in  $\left(0, \frac{\pi}{2}\right)$ . (2)
- **Q.13**. From the differential equation of all lines which makes intercept 3 on *x*-axis. (2)
- **Q.14.** If  $X \sim B(n, p)$  and E(X) = 6 and Var(X) = 4.2, then find n and p.

#### **SECTION – C**

## Attempt any EIGHT of the following questions:

- **Q.15.** If 2  $\tan^{-1}(\cos x) = \tan^{-1}(2 \operatorname{cosec} x)$ , then find the value of x.
- **Q.16.** If angle between the lines represented by  $ax^2 + 2hxy + by^2 = 0$  is equal to the angle between the lines represented by  $2x^2 - 5xy + 3y^2 = 0$ , then show that  $100(h^2 - ab) = (a + b)^2$ . (3)
- Q.17. Find the distance between the parallel lines  $\frac{x}{2} = \frac{y}{-1} = \frac{z}{2}$  and  $\frac{x-1}{2} = \frac{y-1}{-1} = \frac{z-1}{2}$ . (3)

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(3)

[20]

(4)

(4)

- **Q.18.** If A (5, 1, p), B(1, q, p) and C(1, -2, 3) are vertices of a triangle and  $G\left(r, \frac{-4}{3}, \frac{1}{3}\right)$  is its centroid, then find the values of p, q, r by vector method.
- **Q.19.** If  $A(\bar{a})$  and  $B(\bar{b})$  be any two points in the space and  $R(\bar{r})$  be a point on the line segment AB dividing it internally in the ratio m : n then prove that  $\bar{r} = \frac{m\bar{b} + n\bar{a}}{m+n}$ . (3)
- Q.20. Find the vector equation of the plane passing through the point A(-1, 2, -5) and parallel to the vectors 4î-ĵ+3k and î+ĵ-k.

**Q.21.** If 
$$y = e^{m \tan^{-1}x}$$
, then show that  $(1+x^2)\frac{d^2y}{dx^2} + (2x-m)\frac{dy}{dx} = 0$  (3)

**Q.22.** Evaluate: 
$$\int \frac{dx}{2 + \cos x - \sin x}$$
(3)

**Q.23.** Solve 
$$x + y \frac{dy}{dx} = \sec(x^2 + y^2)$$
 (3)

Q.24. A wire of length 36 meters is bent to form a rectangle. Find its dimensions if the area of the rectangle is maximum.
Q.25. Two dice are thrown simultaneously. If X denotes the number of sixes, find the expectation of X.
(3)

- **Q.26.** If a fair coin is tossed 10 times. Find the probability of getting at most six heads. (3)
  - SECTION D

#### Attempt any FIVE of the following questions:

| <b>Q.27.</b> Without using truth table prove that                         |     |
|---|-----|
| $(p \land q) \lor (\sim p \land q) \lor (p \land \sim q) \equiv p \lor q$ | (4) |

Q.28. Solve the following system of equations by the method of inversion x - y + z = 4, 2x + y - 3z = 0, x + y + z = 2

- Q.29. Using vectors prove that the altitudes of a triangle are concurrent.
- Q.30. Solve the L.P.P. by graphical method,

Minimize 
$$z = 8x + 10y$$
  
Subject to  $2x + y \ge 7$ ,  
 $2x + 3y \ge 15$ ,  
 $y \ge 2, x \ge 0$ 
(4)

**Q.31.** If x = f(t) and y = g(t) are differentiable functions of t so that y is differentiable function of x and  $\frac{dx}{dt} \neq 0$ , then prove that:

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\frac{\mathrm{d}y}{\mathrm{d}t}}{\frac{\mathrm{d}x}{\mathrm{d}t}}$$

π

Hence find 
$$\frac{dy}{dx}$$
 if  $x = \sin t$  and  $y = \cos t$ . (4)

**Q.32.** If u and v are differentiable function of *x*, then prove that:

$$\int uv \, dx = u \int v \, dx - \int \left[ \frac{du}{dx} \int v \, dx \right] dx$$
  
Hence evaluate  $\int \log x \, dx$  (4)

**Q.33.** Find the area of region between parabolas  $y^2 = 4ax$  and  $x^2 = 4ay$ .

**Q.34.** Show that: 
$$\int_{0}^{\frac{\pi}{4}} \log(1 + \tan x) \, dx = \frac{\pi}{8} \log 2$$
(4)

3

(4)